Leonardo Senatore (Stanford University)

The Effective Field Theory of Inflation and Multifield Inflation

Large non-Gaussianities

• Standard slow-roll infl.: very Gaussian

Maldacena, JHEP,2003 Acquaviva et al, Nunl.Phys. B,2003

$$\frac{\langle \zeta_{\vec{k}_1} \zeta_{\vec{k}_2} \zeta_{\vec{k}_3} \rangle}{\langle \zeta_{\vec{k}_1} \zeta_{\vec{k}_2} \rangle^{3/2}} \simeq f_{\rm NL} \langle \zeta_{\vec{k}_1} \zeta_{\vec{k}_2} \rangle^{1/2} \sim 10^{-7}$$

- $f_{\rm NL} \sim 10^{-2}$

• DBI inflation

Alishahiha, Silverstein and Tong, Phys.Rev.D70:123505,2004

• Large non-Gaussianities

 $f_{\rm NL} \sim 10^2$

Currently Detectable!

Shape of non-Gaussianities

$$\langle \zeta_{\vec{k}_1} \zeta_{\vec{k}_2} \zeta_{\vec{k}_3} \rangle = (2\pi)^3 \delta^{(3)} \left(\sum_i \vec{k}_i\right) F\left(\frac{k_2}{k_1}, \frac{k_3}{k_1}\right)$$

• What are the generic signatures?



The Effective Field Theory of Inflation

with C. Cheung, P. Creminelli, L. Fitzpatrick, J. Kaplan JHEP 0803:014,2008

The Effective Field Theory

Inflation: Quasi dS phase with a broken time-translation.

Inflation: theory of the Goldstone. $\pi \rightarrow \pi - \delta t$

$$S_{\pi} = \int d^4x \,\sqrt{-g} \left[M_{\rm Pl}^2 \dot{H} (\dot{\pi}^2 - (\partial_i \pi)^2) + M_2^4 \left(\dot{\pi}^2 + \dot{\pi}^3 - \dot{\pi} (\partial_i \pi)^2 \right) - M_3^4 \dot{\pi}^3 + \dots \right]$$

• Analogous of the (more important!) Chiral Lagrangian for the Pions S.Weinberg PRL 17, 1966 $\pi \sim \delta \phi$

- All single field models are unified (Ghost Inflation, DBI inflation, ...); prove theorems:
 Theorem: In single clock models, only Inflation can produce more than 10 e-foldings of scale invariant fluct.
- What is forced by symmetries and large signatures are explicit:
 - The spatial kinetic term: pathologies for : $\dot{H} > 0$ add $\delta E^2 \Rightarrow$

with Baumann and Zaldarriaga **1101:3320** [hep-th]

$$\left(\partial_i^2 \pi\right)^2 \quad \Rightarrow \quad w < -1$$

with Creminelli, Luty and Nicolis, JHEP 0612

• Connection between c_s and Non-Gaussianities: $\dot{\pi}^2 - c_s^2 (\partial_i \pi)^2$, NG: $f_{NL}^{\text{non-loc.}} \sim \frac{1}{c_s^2}$ • Large interactions are allowed \Longrightarrow Large non-Gaussianities! $\dot{\pi} (\nabla \pi)^2$

Large non-Gaussianites

with Smith and Zaldarriaga, JCAP1001:028,2010



Let's look at the data



\sim No detection \approx

With Smith and Zaldarriaga, JCAP0909:006,2009 JCAP1001:028,2010

Optimal analysis of WMAP data (foreground template corrections) are ~ compatible with Gaussianity

Optimal limits on NG

 $-10 < f_{NL}^{local} < 74$ at 95% C.L. (-5 < $f_{NL}^{local} < 59$ at 95% C.L.) Komatsu et al. WMAP 7yr

after combining with LSS Slosar *et al*. JCAP 0808:031, 2008

 $-214 < f_{NL}^{equil.} < 266 \quad at 95\% \text{ C.L.}$ -410 < $f_{NL}^{orthog.} < 6 \quad at 95\% \text{ C.L.}$

Komatsu et al. WMAP 7yr



Friday, May 13, 2011

(Optimal) Limits on the parameters of the Lagrangian $S_{\pi} = \int d^4x \sqrt{-g} \left[M_{\rm Pl}^2 \dot{H} (\dot{\pi}^2 - (\partial_i \pi)^2) + M_2^4 (\dot{\pi}^2 + \dot{\pi}^3 - \dot{\pi} (\partial_i \pi)^2) - M_3^4 \dot{\pi}^3 + \dots \right]$

- Limits on f_{NL} 's get translated into limits on the parameters
- For models not-very-close to de Sitter (like DBI): c_s , \tilde{c}_3



With Smith and Zaldarriaga, **JCAP1001:028,2010**



- Close to de Sitter. $d_1 \, \delta g^{00} \delta K_i^i$
- Dispertion relation: $\omega^2 = c_s^2 k^2$

$$c_s^2 = d_1 \frac{H}{M} \ll 1$$



With Smith and Zaldarriaga, JCAP1001:028,2010

- Close to de Sitter. $d_2 \, \delta K_i^{i2}$ Dispertion relation: $\omega^2 = (d_2 + d_3) \frac{k^4}{M^2}$



With Smith and Zaldarriaga, JCAP1001:028,2010

- Close to de Sitter.
- Negative c_s^2 due to $d_1 < 0$ $c_s^2 = d_1$

$$c_s^2 = d_1 \frac{H}{M} \ll 1$$

• Ruled out at 95% CL.



With Smith and Zaldarriaga, **JCAP1001:028,2010**

- Close to de Sitter.
- Negative c_s^2 due to $\dot{H} > 0$ $\dot{H}M_{\rm Pl}^2(\partial_i \pi)^2$

• Ruled out at 95% CL.



With Smith and Zaldarriaga, JCAP1001:028,2010

$$S_{\pi} = \int d^4x \,\sqrt{-g} \left[M_{\rm Pl}^2 \dot{H} (\dot{\pi}^2 - (\partial_i \pi)^2) + M_2^4 \left(\dot{\pi}^2 + \dot{\pi}^3 - \dot{\pi} (\partial_i \pi)^2 \right) - M_3^4 \dot{\pi}^3 + \dots \right]$$

• Thanks to the EFT: A qualitatively new (and superior) way to use the cosmological data



This was about 3-point function. What about 4-point function?

with M. Zaldarriaga JCAP 2011 [hep-th]

Another New Signature: JCAP 2011 A large 4-point function without a larger 3-point function

• Large 4-point: Symmetries forces to have a leading 3-point function but for one case:



- Protected by a approximate symmetry $\Rightarrow \pi \to -\pi$
- Huge amount of information: function of 5 variables
- Looking it in the data

with Smith and Zaldarriaga in progress



Effective Field Theory of Multifield Inflation

with M. Zaldarriaga **1009.2093 hep-th**

The Effective Field Theory for Multifield Inflation

In the same Unitary Gauge, consider another massless scalar field σ [Classification: approximate shift symmetry:

- Abelian
- Non-Abelian
- Supersymmetry]

The add conversion into curvature perturbations



The Effective Field Theory for Multifield Inflation

In the same Unitary Gauge, consider another massless scalar field σ [Classification:





- Supersymmetry]

The add conversion into curvature perturbations



Reintroducing the Goldstone

• Quadratic Lagrangian

$$S^{(2)} = \int d^4x \sqrt{-g} \left[(2M_2^4 - M_{\rm Pl}^2 \dot{H}) \dot{\pi}^2 + M_{\rm Pl}^2 \dot{H} \frac{(\partial_i \pi)^2}{a^2} + 2\tilde{M}_1^2 \dot{\pi} \dot{\sigma} + (-e_1 + e_2) \dot{\sigma}^2 + e_1 \frac{(\partial_i \sigma)^2}{a^2} + \dots \right]$$

- Cubic Lagrangian ...
- Quartic Lagrangian
- Notice:

 - Small π speed of sound: Large coupling $M^4 \dot{\pi}^2 \rightarrow M^4 \dot{\pi} (\partial_i \pi)^2$ Small σ speed of sound: Large coupling $(-e_1 + e_2) \dot{\sigma}^2 \rightarrow e_2 (\partial_i \pi \partial_i \sigma) \dot{\sigma}$
 - Time-kinetic mixing σ - π .

Reintroducing the Goldstone

• Quadratic Lagrangian

$$S^{(2)} = \int d^4x \sqrt{-g} \left[(2M_2^4 - M_{\rm Pl}^2 \dot{H}) \dot{\pi}^2 + M_{\rm Pl}^2 \dot{H} \frac{(\partial_i \pi)^2}{a^2} + 2\tilde{M}_1^2 \dot{\pi} \dot{\sigma} + (-e_1 + e_2) \dot{\sigma}^2 + e_1 \frac{(\partial_i \sigma)^2}{a^2} + \dots \right]$$

- Cubic Lagrangian ...
- Quartic Lagrangian
- Notice:

 - Small π speed of sound: Large coupling $M^4 \dot{\pi}^2 \rightarrow M^4 \dot{\pi} (\partial_i \pi)^2$ Small σ speed of sound: Large coupling $(-e_1 + e_2) \dot{\sigma}^2 \rightarrow e_2 (\partial_i \pi \partial_i \sigma) \dot{\sigma}$
 - Time-kinetic mixing σ - π .

- In multifield inflation:
 - -Impose symm. $\sigma \rightarrow -\sigma$
 - -Approximate Lorentz invariance \Rightarrow kill σ^3 terms
- Large 4-point function $\dot{\sigma}^4$, $\dot{\sigma}^2(\partial_i \sigma)^2$, $(\partial_i \sigma)^4$, $\sigma^2(\partial \sigma)^2 = \sigma^4$

with M. Zaldarriaga

1009.2093 hep-th

• and it is a function of 5 variables!



• Analysis in progress

with Smith and Zaldarriaga in progress

On the non-Abelian case

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- Not exactly a shift symmetry: $\sigma^2 (\partial \sigma)^2$
- Building Blocks: $[t_i, t_j] = iC_{ijk}t_k$ $[t_i, x_a] = iC_{iab}x_b$ $[x_a, x_b] = iC_{abi}t_i + iC_{abc}x_c$

$$D_{a\mu} = \partial_{\mu}\sigma_{a} + \frac{1}{2}C_{abc}\sigma_{b}\partial_{\mu}\sigma_{c} + \frac{1}{6}\left(C_{cde}C_{bea} + C_{cdi}C_{bia}\right)\sigma_{b}\sigma_{c}\partial_{\mu}\sigma_{d} + \mathcal{O}(\sigma^{3}\partial_{\mu}\sigma)$$

• Good Transformation Properties:

$$D_{\mu} \equiv D_{a\mu} x_{a}$$
$$D'_{\mu} = h\left(\sigma(x), g\right) D_{\mu} h\left(\sigma(x), g\right)^{-1}$$

• Lagrangian:

$$S_{\pi\sigma} = \int d^4x \sqrt{-g} \qquad \text{Tr} \left[F_1^2 D_\mu D^\mu + F_2^2 D^0 D^0 + 2F_2^2 \partial_\mu \pi D^\mu D^0 - 2F_3^3 \dot{\pi} D^0 + F_3^3 (\partial_\mu \pi)^2 D^0 - 2F_4^2 \dot{\pi} D_\mu D^\mu - 2F_5^2 \dot{\pi} D^0 D^0 + \bar{F}_1 D_\mu D^\mu D^0 + \bar{F}_2 D^0 D^0 D^0 + \dots \right]$$

On the non-Abelian case

9

TT9

- Usual operators and maybe something else:
- No $\sigma(\partial\sigma)^2$: $C_{abc}\sigma_a(\partial\sigma_b)(\partial\sigma_c) = 0$
- Sensitive to only one field (for adiabatic fluctuations):

$$\frac{\partial \zeta}{\partial \sigma_I} \bigg|_0 \sigma_I(x) = \frac{\partial \zeta}{\partial \sigma_K} \bigg|_0 \mathscr{D}(h)_{KI}^{-1} \mathscr{D}(h)_{IJ} \sigma_J(x) = \frac{\widetilde{\partial \zeta}}{\partial \sigma_1} \bigg|_0 \sigma_1'$$

• Easy to suppress the standard opt's:

$$\dot{\sigma}^3$$
, $\dot{\sigma}(\partial_i \sigma)^2$, only if $\operatorname{Tr}[x_a x_a x_a] \neq 0$

 $n \mid$

• Mixed iso-adiabatic becomes large:

$$\langle \zeta \zeta \zeta_{\rm iso} \zeta_{\rm iso} \rangle \Rightarrow \sigma^2 (\partial \sigma)^2 \Rightarrow \epsilon_{\rm iso}^2 \frac{\mathcal{L}_4}{\mathcal{L}_2} \Big|_{E \sim H} \sim \epsilon_{\rm iso}^2 \frac{\sigma_c^2}{\Lambda_U^2} \sim \epsilon_{\rm iso}^2 \frac{H^2}{\Lambda_U^2}$$

$$\langle \zeta \zeta \zeta \zeta \rangle \implies (\partial \sigma)^4 \implies \frac{\mathcal{L}_4}{\mathcal{L}_2}\Big|_{E \sim H} \sim \frac{H^2 \sigma_c^2}{\Lambda_U^4} \sim \frac{H^4}{\Lambda_U^4}$$

• A remarkable Signature

SuperSymmetric case

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- Chiral Multiplet $\Sigma \supset \sigma, \psi_{\sigma}$, with shift symmetry $K = (\Sigma + \Sigma^{\dagger})^2$
- In dS, propagator modified at $E \leq H$
- Because of week coupling, radiative corrections stop at $E \sim \lambda H$ with $W = \lambda \Sigma^3$
- no relevant mass is generated
- Leading interaction $\lambda^2 {
 m Im}(\sigma)^4$ with no ${
 m Im}(\sigma)^3$
- Another way to get detectable $\tau_{NL}^{\rm loc}$ and no $f_{NL}^{\rm loc}$

MultiField

with M. Zaldarriaga **1009.2093 hep-th**

Operator	Dispe	rsion	Type	Origin	Squeezed L.
	$w = c_s k$	$w \propto k^2$			
$\dot{\sigma}^4 \;,\; \dot{\sigma}^2 (\partial_i \sigma)^2 \;, (\partial_i \sigma)^4$	Х		Ad., Iso.	Ab., non-Ab.	
$(\partial_{\mu}\sigma)^4$	Х		Ad., Iso.	Ab., non-Ab.	
σ^4	Х	Х	Ad., Iso.	Ab. _s , non-Ab. _s , S.*	Х
$\dot{\sigma}\sigma^3$	Х	Х	Ad., Iso.	$Ab{s}^{\dagger}, \text{ non-}Ab{s}^{\dagger}.$	Х
$\sigma^2 \dot{\sigma}^2 \;, \sigma^2 (\partial_i \sigma)^2$	Х	$X^{\dagger \star}$	Ad. ^{\dagger*} , Iso.	non-Ab, Ab. $_{s}^{\dagger \star}$, non-Ab. $_{s}^{\dagger \star}$,	Х
$\sigma^2 (\partial_\mu \sigma)^2$	Х		Ad. ^{\dagger*} , Iso.	non-Ab, Ab. $_{s}^{\dagger \star}$, non-Ab. $_{s}^{\dagger \star}$, S.*	Х
$\sigma(\partial\sigma)^3$	Х		Iso.	non-Ab. $_{s}^{\star}$.	Х
$\dot{\sigma}^3 \;,\; \dot{\sigma} (\partial_i \sigma)^2$	Х		Ad., Iso.	Ab., non-Ab.	
$\dot{\sigma}(\partial_i\sigma)^2 \ , \partial_j^2\sigma(\partial_i\sigma)^2$		Х	Ad., Iso.	Ab.	
σ^{3}	Х	Х	Ad., Iso.	Abs, non- Abs , S, R	Х
$\dot{\sigma}\sigma^2$	Х	Х	Ad., Iso.	Abs, non- Abs	Х
$\sigma \dot{\sigma}^2 \;,\; \sigma (\partial_i \sigma)^2$	Х	Х	Ad., Iso.	$Ab{s}^{\dagger \star}$, non- $Ab{s}^{\dagger \star}$	Х
$\sigma(\partial_\mu\sigma)^2$	X		Ad., Iso.	Ab. $_{s}^{\dagger \star}$, non-Ab. $_{s}^{\dagger \star}$.	X

Operator	Dispersion		Squeezed L.
	$w = c_s k$	$w \propto k^2$	
$\dot{\pi}^4$	Х		
$(\partial_j^2 \pi)^4$, $\dot{\pi} (\partial_j^2 \pi)^3$,		Х	
$\dot{\pi}^3$, $\dot{\pi}(\partial_i \pi)^2$	Х		
$\dot{\pi}(\partial_i\pi)^2, \partial_j^2\pi(\partial_i\pi)^2$		Х	

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Operator	Dispe	rsion	Type	Origin	Squeezed L.
	$w = c_s k$	$w \propto k^2$			
$\dot{\sigma}^4 \ , \ \dot{\sigma}^2 (\partial_i \sigma)^2 \ , (\partial_i \sigma)^4$	V		Ad., Iso.	Ab., non-Ab.	
$(\partial_{\mu}\sigma)^4$	Х		Ad., Iso.	Ab., non-Ab.	
σ^4	Х	Х	Ad., Iso.	Ab. _s , non-Ab. _s , S.*	Х
$\dot{\sigma}\sigma^3$	Х	Х	Ad., Iso.	$Ab{s}^{\dagger}, \text{ non-}Ab{s}^{\dagger}.$	Х
$\sigma^2 \dot{\sigma}^2 \;, \sigma^2 (\partial_i \sigma)^2$	Х	$X^{\dagger \star}$	Ad. ^{$\dagger \star$} , Iso.	non-Ab, Ab. $_{s}^{\dagger \star}$, non-Ab. $_{s}^{\dagger \star}$,	Х
$\sigma^2 (\partial_\mu \sigma)^2$	Х		Ad. ^{\dagger*} , Iso.	non-Ab, Ab. $_{s}^{\dagger \star}$, non-Ab. $_{s}^{\dagger \star}$, S.*	Х
$\sigma(\partial\sigma)^3$	X		Iso.	non-Ab. $_{s}^{\star}$.	Х
$\dot{\sigma}^3 \ , \ \dot{\sigma} (\partial_i \sigma)^2$	X		Ad., Iso.	Ab., non-Ab.	
$\dot{\sigma}(\partial_i\sigma)^2 \ , \partial_j^2\sigma(\partial_i\sigma)^2$		Х	Ad., Iso.	Ab.	
σ^{3}	Х	Х	Ad., Iso.	Ab. $_s$, non-Ab. $_s$, S, R	Х
$\dot{\sigma}\sigma^2$	Х	Х	Ad., Iso.	Abs, non-Abs	Х
$\sigma \dot{\sigma}^2 \;,\; \sigma (\partial_i \sigma)^2$	Х	Х	Ad., Iso.	$Ab{s}^{\dagger \star}, \text{ non-}Ab{s}^{\dagger \star}$	Х
$\sigma(\partial_{\mu}\sigma)^2$	X		Ad., Iso.	Ab. $^{\dagger\star}_s$, non-Ab. $^{\dagger\star}_s$.	X

Single Field

Operator	Dispersion		Squeezed L.
	$w = c_s k$	$w \propto k^2$	
$\dot{\pi}^4$	Х		
$(\partial_j^2 \pi)^4$, $\dot{\pi} (\partial_j^2 \pi)^3$,		Х	
$\dot{\pi}^3$, $\dot{\pi}(\partial_i \pi)^2$	Х		
$\dot{\pi}(\partial_i\pi)^2 , \partial_j^2\pi(\partial_i\pi)^2$		Х	

MultiField

with M. Zaldarriaga **1009.2093 hep-th**

Operator	Dispe	rsien	Type	Origin	Squeezed L.
	$w = c_s k$	$w \propto k^2$			
$\dot{\sigma}^4 \;,\; \dot{\sigma}^2 (\partial_i \sigma)^2 \;, (\partial_i \sigma)^4 \;$	Х		Ad., Iso.	Ab., non-Ab.	
$(\partial_{\mu}\sigma)^4$	Х		Ad., Iso.	Ab., non-Ab.	
σ^4	Х	Х	Ad., Iso.	Ab. _s , non-Ab. _s , S.*	Х
$\dot{\sigma}\sigma^3$	Х	Х	Ad., Iso.	$Ab{s}^{\dagger}, \text{ non-}Ab{s}^{\dagger}.$	Х
$\sigma^2 \dot{\sigma}^2 \;, \sigma^2 (\partial_i \sigma)^2$	Х	$X^{\dagger \star}$	Ad. ^{†*} , Iso.	non-Ab, Ab. $_{s}^{\dagger \star}$, non-Ab. $_{s}^{\dagger \star}$,	Х
$\sigma^2 (\partial_\mu \sigma)^2$	Х		Ad. ^{†*} , Iso.	non-Ab, Ab. $_{s}^{\dagger \star}$, non-Ab. $_{s}^{\dagger \star}$, S.*	Х
$\sigma(\partial\sigma)^3$	Х		Iso.	non-Ab. $_{s}^{\star}$.	Х
$\dot{\sigma}^3 \ , \ \dot{\sigma} (\partial_i \sigma)^2$	Х		Ad., Iso.	Ab., non-Ab.	
$\dot{\sigma}(\partial_i\sigma)^2 \ , \partial_j^2\sigma(\partial_i\sigma)^2$		Х	Ad., Iso.	Ab.	
σ^{3}	Х	Х	Ad., Iso.	Ab. $_s$, non-Ab. $_s$, S, R	Х
$\dot{\sigma}\sigma^2$	Х	Х	Ad., Iso.	Abs, non- Abs	Х
$\sigma \dot{\sigma}^2 \;,\; \sigma (\partial_i \sigma)^2$	Х	Х	Ad., Iso.	$Ab{s}^{\dagger\star}$, non- $Ab{s}^{\dagger\star}$	Х
$\sigma (\partial_\mu \sigma)^2$	X		Ad., Iso.	Ab. $_{s}^{\dagger \star}$, non-Ab. $_{s}^{\dagger \star}$.	X

Operator	Dispersion		Squeezed L.
	$w = c_s k$	$w \propto k^2$	
$\dot{\pi}^4$	Х		
$(\partial_j^2 \pi)^4$, $\dot{\pi} (\partial_j^2 \pi)^3$,		Х	
$\dot{\pi}^3 , \dot{\pi} (\partial_i \pi)^2$	Х		
$\dot{\pi}(\partial_i\pi)^2 , \partial_j^2\pi(\partial_i\pi)^2$		Х	

MultiField

with M. Zaldarriaga **1009.2093 hep-th**

Operator	Dispe	rsion	Туре	Origin	Squeezed L.
	$w = c_s k$	$w \propto k^2$			
$\dot{\sigma}^4 \ , \ \dot{\sigma}^2 (\partial_i \sigma)^2 \ , (\partial_i \sigma)^4$	Х		Ad., Iso.	Ab., non-Ab.	
$(\partial_{\mu}\sigma)^4$	Х		Ad., Iso.	Ab., non-Ab.	
σ^4	Х	Х	Ad., Iso.	Ab. _s , non-Ab. _s , S.*	Х
$\dot{\sigma}\sigma^3$	Х	Х	Ad., Iso.	$Ab{s}^{\dagger}, \text{ non-}Ab{s}^{\dagger}.$	Х
$\sigma^2 \dot{\sigma}^2 \;, \sigma^2 (\partial_i \sigma)^2$	Х	$X^{\dagger \star}$	Ad. ^{$\dagger \star$} , Iso.	non-Ab, Ab. $_{s}^{\dagger\star}$, non-Ab. $_{s}^{\dagger\star}$,	Х
$\sigma^2 (\partial_\mu \sigma)^2$	Х		Ad. ^{$\dagger \star$} , Iso.	non-Ab, Ab. $_{s}^{\dagger \star}$, non-Ab. $_{s}^{\dagger \star}$, S.*	Х
$\sigma(\partial\sigma)^3$	Х		Iso.	non-Ab. $_{s}^{\star}$.	Х
$\dot{\sigma}^3 \ , \ \dot{\sigma} (\partial_i \sigma)^2$	Х		Ad., Iso.	Ab., non-Ab.	
$\dot{\sigma}(\partial_i\sigma)^2 \ , \partial_j^2\sigma(\partial_i\sigma)^2$		Х	Ad., Iso.	Ab.	
σ^3	Х	Х	Ad., Iso.	Ab. $_s$, non-Ab. $_s$, S, R	Х
$\dot{\sigma}\sigma^2$	Х	Х	Ad., Iso.	Abs, non-Abs	Х
$\sigma \dot{\sigma}^2 \;,\; \sigma (\partial_i \sigma)^2$	Х	Х	Ad., Iso.	$Ab{s}^{\dagger\star}$, non- $Ab{s}^{\dagger\star}$	Х
$\sigma(\partial_{\mu}\sigma)^2$	Х		Ad., Iso.	Ab. $_{s}^{\dagger \star}$, non-Ab. $_{s}^{\dagger \star}$.	Х

Single Field

Operator	Dispersion		Squeezed L.
	$w = c_s k$	$w \propto k^2$	
$\dot{\pi}^4$	Х		
$(\partial_j^2 \pi)^4$, $\dot{\pi} (\partial_j^2 \pi)^3$,		Х	
$\dot{\pi}^3$, $\dot{\pi}(\partial_i \pi)^2$	Х		
$\dot{\pi}(\partial_i\pi)^2 , \partial_j^2\pi(\partial_i\pi)^2$		Х	

MultiField

with M. Zaldarriaga **1009.2093 hep-th**

Operator	Dispe	rsion	Type	Origin	Squeezed L.
	$w = c_s k$	$w \propto k^2$			
$\dot{\sigma}^4 \;,\; \dot{\sigma}^2 (\partial_i \sigma)^2 \;, (\partial_i \sigma)^4$	Х		Ad., Iso.	Ab., non-Ab.	
$(\partial_{\mu}\sigma)^4$	Х		Ad., Iso.	Ab., non-Ab.	
σ^4	Х	Х	Ad., Iso.	Ab., per Ab., S^*	Х
$\dot{\sigma}\sigma^3$	Х	Х	Ad., Iso.	$Ab{s}^{\dagger}, \text{ non-}Ab{s}^{\dagger}.$	Х
$\sigma^2 \dot{\sigma}^2 \;, \sigma^2 (\partial_i \sigma)^2$	Х	$X^{\dagger \star}$	Ad. ^{\dagger*} , Iso.	non Ab, Ab. $_{s}^{\dagger \star}$, non-Ab. $_{s}^{\dagger \star}$,	Х
$\sigma^2 (\partial_\mu \sigma)^2$	Х		Ad. ^{\dagger*} , Iso.	non-Ab, Ab., in Ab., S.*	Х
$\sigma(\partial\sigma)^3$	Х		Iso.	non-Ab. $_{s}^{\star}$.	Х
$\dot{\sigma}^3 \ , \ \dot{\sigma} (\partial_i \sigma)^2$	Х		Ad., Iso.	Ab., non-Ab.	
$\dot{\sigma}(\partial_i\sigma)^2 \ , \partial_j^2\sigma(\partial_i\sigma)^2$		Х	Ad., Iso.	Ab.	
σ^{3}	Х	Х	Ad., Iso.	$Ab_{.s}, non-Ab_{.s}, S, R$	Х
$\dot{\sigma}\sigma^2$	Х	Х	Ad., Iso.	Abs, non-Abs	Х
$\sigma \dot{\sigma}^2 \;,\; \sigma (\partial_i \sigma)^2$	Х	Х	Ad., Iso.	$Ab{s}^{\dagger\star}, \text{ non-}Ab{s}^{\dagger\star}$	Х
$\sigma(\partial_\mu\sigma)^2$	Х		Ad., Iso.	Ab. $_{s}^{\dagger\star}$, non-Ab. $_{s}^{\dagger\star}$.	Х

Operator	Dispersion		Squeezed L.
	$w = c_s k$	$w \propto k^2$	
$\dot{\pi}^4$	Х		
$(\partial_j^2 \pi)^4$, $\dot{\pi} (\partial_j^2 \pi)^3$,		Х	
$\dot{\pi}^3$, $\dot{\pi}(\partial_i \pi)^2$	Х		
$\dot{\pi}(\partial_i \pi)^2 , \partial_j^2 \pi (\partial_i \pi)^2$		Х	

MultiField

with M. Zaldarriaga **1009.2093 hep-th**

Operator	Dispe	rsion	Type	Origin	Squeezed L.
	$w = c_s k$	$w \propto k^2$			
$\dot{\sigma}^4 \;,\; \dot{\sigma}^2 (\partial_i \sigma)^2 \;, (\partial_i \sigma)^4 \;$	Х		Ad., Iso.	Ab., non-Ab.	
$(\partial_{\mu}\sigma)^4$	Х		Ad., Iso.	Ab., non-Ab.	
σ^4	Х	Х	Ad., Iso.	Ab. _s , non-Ab. _s , S.*	Х
$\dot{\sigma}\sigma^3$	Х	Х	Ad., Iso.	$Ab{s}^{\dagger}, \text{ non-}Ab{s}^{\dagger}.$	Х
$\sigma^2 \dot{\sigma}^2 \;, \sigma^2 (\partial_i \sigma)^2$	Х	$X^{\dagger \star}$	Ad. ^{\dagger*} , Iso.	non-Ab, Ab. $_{s}^{\dagger\star}$, non-Ab. $_{s}^{\dagger\star}$,	Х
$\sigma^2 (\partial_\mu \sigma)^2$	Х		Ad. ^{$\dagger \star$} , Iso.	non-Ab, Ab. $_{s}^{\dagger \star}$, non-Ab. $_{s}^{\dagger \star}$, S.*	Х
$\sigma(\partial\sigma)^3$	Х		Iso.	non-Ab. $_{s}^{\star}$.	X
$\dot{\sigma}^3 \ , \ \dot{\sigma} (\partial_i \sigma)^2$	Х		Ad., Iso.	Ab., non-Ab.	
$\dot{\sigma}(\partial_i\sigma)^2 \ , \partial_j^2\sigma(\partial_i\sigma)^2$		Х	Ad., Iso.	Ab.	
σ^{3}	Х	Х	Ad., Iso.	Ab. $_s$, non-Ab. $_s$, S, R	Х
$\dot{\sigma}\sigma^2$	Х	Х	Ad., Iso.	Abs, non- Abs	Х
$\sigma \dot{\sigma}^2 \;,\; \sigma (\partial_i \sigma)^2$	Х	Х	Ad., Iso.	$Ab{s}^{\dagger\star}$, non- $Ab{s}^{\dagger\star}$	Х
$\sigma(\partial_\mu\sigma)^2$	X		Ad., Iso.	$Ab{s}^{\dagger\star}$, non- $Ab{s}^{\dagger\star}$.	X

Operator	Dispersion		Squeezed L.
	$w = c_s k$	$w \propto k^2$	
$\dot{\pi}^4$	Х		
$(\partial_j^2 \pi)^4$, $\dot{\pi} (\partial_j^2 \pi)^3$,		Х	
$\dot{\pi}^3 , \dot{\pi} (\partial_i \pi)^2$	Х		
$\dot{\pi}(\partial_i\pi)^2 , \partial_j^2\pi(\partial_i\pi)^2$		Х	

MultiField

with M. Zaldarriaga **1009.2093 hep-th**

Operator	Dispersion		Туре	Origin		Squeezed L.
	$w = c_s k$	$w \propto k^2$				
$\dot{\sigma}^4 \ , \ \dot{\sigma}^2 (\partial_i \sigma)^2 \ , (\partial_i \sigma)^4$	Х		Ad., Iso.	Ab., non-Ab.		
$(\partial_\mu \sigma)^4$	Х		Ad., Iso.	Ab., non-Ab.		
σ^4	Х	Х	Ad., Iso.	Ab	h_{s} , non-Ab. $_{s}$, S.*	Х
$\dot{\sigma}\sigma^3$	Х	Х	Ad., Iso.	A	$Ab{s}^{\dagger}, \text{ non-}Ab{s}^{\dagger}.$	Х
$\sigma^2 \dot{\sigma}^2 \;, \sigma^2 (\partial_i \sigma)^2$	Х	X [†] *	Ad. ^{\dagger*} , Iso.	non-A	b, Ab. $_{s}^{\dagger \star}$, non-Ab. $_{s}^{\dagger \star}$	х, Х
$\sigma^2 (\partial_\mu \sigma)^2$	Х		Ad. ^{\dagger*} , Iso.	non-Ab, Ab. $_{s}^{\dagger \star}$, non-Ab. $_{s}^{\dagger \star}$, S.*		S.* X
$\sigma(\partial\sigma)^3$	Х		Iso.	non-Ab. $_{s}^{\star}$.		X
$\dot{\sigma}^3 \;,\; \dot{\sigma} (\partial_i \sigma)^2$	X		Ad., J. p.	Ab., non-Ab.		
$\dot{\sigma}(\partial_i\sigma)^2 \ , \partial_j^2\sigma(\partial_i\sigma)^2$		Х	Ad., Isp.	Ab.		
σ^3	Х	Х	Ad., Isp.	Ab. $_s$, non-Ab. $_s$, S, R		X
$\dot{\sigma}\sigma^2$	Х	Х	Ad., Isp.	$Abs, \text{ non-Ab.}_s$		X
$\sigma \dot{\sigma}^2 \;,\; \sigma (\partial_i \sigma)^2$	Х	Х	Ad., Is .	$Ab{s}^{\dagger \star}, \text{ non-}Ab{s}^{\dagger \star}$		X
$\sigma (\partial_{\mu} \sigma)^2$	Х		Ad., Isc.	A	b. ^{†*} , non-Ab. ^{†*} .	X
Single Field	Field Operator		Di persion Squeezed L.			
			$w = c_s k$	$w \propto k^2$		
	$\dot{\pi}^4$		X			You can tell the
	$(\partial_j^2 \pi)^4$, $\dot{\pi} (\partial_j^2 \pi)^3$,.			X		anart
	 	<u> </u>				ipari.

Х

Х

 $\dot{\pi}^3$, $\dot{\pi}(\partial_i \pi)^2$

 $\dot{\pi}(\partial_i \pi)^2$, $\partial_i^2 \pi (\partial_i \pi)^2$









Theory

- Adding Gauge Bosons and Fermions
- Higher derivative interactions in π , ex: $(\partial^4 \pi)^3$

Bartolo, Fasiello, Matarrese, Riotto **2010, 2010** Creminelli, D'Amico, Norena, Trincherini **2010** with Behbahani, Mirbabayi **in progress**

• Relaxing the shift-symmetry of $~\pi$

with Dimarsky, Behbahani, Mirbabayi in progress

- Backreaction from additional Fields on $\,\pi\,$, EFT for thermal and trapped Inflat.

 $S_{\rm int} = -\int d^4x \mathcal{O}(x)\pi(x),$

with Nacir, Porto, and Zaldarriaga **in progress**

Conclusions

Inflation: Exploring the beginning of the Universe

• Many observational data, and many more to come



- Power Spectra: scalar and gravity waves
- Non-Gaussianities: Richness of information
 - Smoking Gun
 - Interactions

Fundamental Theory

• Learning about the origin of the Universe and the high energy physics

$$S_{\pi} = \int d^4x \,\sqrt{-g} \left[M_{\rm Pl}^2 \dot{H} (\dot{\pi}^2 - (\partial_i \pi)^2) + M_2^4 \left(\dot{\pi}^2 + \dot{\pi}^3 - \dot{\pi} (\partial_i \pi)^2 \right) - M_3^4 \dot{\pi}^3 + \dots \right]$$



DBI inflation ($\tilde{c}_3 = 3(1-c_s^2)$

Equilateral: $\partial_i \pi (\partial_i \pi)^2$

 $F(\frac{k_2}{k_1}, \frac{k_3}{k_1})$